

V.P.& R.P.T.P.Science College, Vallabh Vidyanagar.

Internal Test

B.Sc. Semester - I

US01CMTH01

( ANALYTIC GEOMETRY AND COMPLEX NUMBERS )

Date. 8/10/2015 ; Thursday

1.30 p.m. to 2.30 p.m.

Maximum Marks: 25

Que.1 Fill in the blanks.

3

- (1) Parametric equation for  $x^{2/3} - y^{2/3} = a^{2/3}$  are .....
- (a)  $x = a \cos^3 \theta ; y = a \sin^3 \theta$     (b)  $x = a \sec^3 \theta ; y = a \tan^3 \theta$   
 (c)  $x = \cos^3 \theta ; y = \sin^3 \theta$         (d)  $x = a \tan^3 \theta ; y = a \sec^3 \theta$
- (2) Polar equation of vertical line through the point  $(-3, 180^0)$  is .....
- (a)  $3 = r \cos \theta$     (b)  $3 = r \sin \theta$     (c)  $3 = -r \sin \theta$     (d)  $3 = -r \cos \theta$
- (3) For  $z = 1 + \cos \alpha + i \sin \alpha$ , amp  $z =$  .....
- (a)  $\frac{\pi}{2}$     (b)  $\frac{\pi}{2} - \frac{\alpha}{2}$     (c)  $\frac{\alpha}{2}$     (d)  $\frac{\pi}{2} + \frac{\alpha}{2}$



Que.2 Answer the following ( Any Two )

4

- (1) Find any one oblique asymptote, for the curve given by  $x = t + \frac{1}{t^2} ; y = t - \frac{1}{t^2}$ .
- (2) If  $\sin \alpha + \sin \beta + \sin \gamma = \cos \alpha + \cos \beta + \cos \gamma = 0$  then prove that  $\sin 3\alpha + \sin 3\beta + \sin 3\gamma = 3 \sin(\alpha + \beta + \gamma)$
- (3) Find polar equation of circle centre at  $(5, 210^0)$  and radius is 2.

- Que.3 (a) If a curve is given by  $x = f(t) ; y = g(t)$  and that both  $x$  and  $y$  get numerically large as  $t$  approaches some number, say  $a$ . Then an oblique asymptote to the curve, if it exist, is given by  $y = mx + c$ , where  $m = \lim_{t \rightarrow a} \frac{dy}{dx}$  and  $c = \lim_{t \rightarrow a} (y - mx)$ .
- (b) A circle of radius  $a$  rolls along a line without sliding. Show that the path traced by a point on the radius  $b$  units ( $b < a$ ) from the centre is given by  $x = a\theta - b \sin \theta ; y = a - b \cos \theta$ .

3

3

OR

Que.3 (a) Sketch the curve given by  $y = \frac{(x-1)(x+2)}{x(x+4)}$ .

5

(b) Determine the extent for the curve given by  $x = 4t^2 - 4t ; y = 1 - 4t^2$ .

1

Que.4 (a) In usual notation prove that  $r = \frac{pe}{1 \pm e \sin \theta}$ .

5

(b) Find the perpendicular distance of  $4 = r(\cos \theta - \sin \theta)$  from the pole.

1

OR

Que.4 (a) Prove that equation of line not passing through the pole is  $p = r \cos(\theta - \omega)$ , where  $(p, \omega)$  is the foot of the perpendicular from the pole. Also find equation of horizontal line.

3

(b) If any straight line through the pole meets the circle  $r^2 - 2rd \cos(\theta - \alpha) + d^2 - a^2 = 0$  at point P and Q. Then prove that  $OP \cdot OQ = d^2 - a^2$ .

3

Que.5 (a) State and prove De-Moivre's theorem.

5

(b) Find the modulus of  $\frac{(3 + \sqrt{2}i)^2}{1 + 3i}$ .

1

OR

Que.5 (a) Express  $\frac{\sin 6\theta}{\sin \theta}$  as a polynomial in  $\cos \theta$ .

3

(b) Expand  $\cos^8 \theta$  in a series of cosines of multiples of  $\theta$ .

3

